

# An Algorithm for Allocating Sponsored Recommendations and Content: Unifying Programmatic Advertising and Recommender Systems

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# An Algorithm for Allocating Sponsored Recommendations and Content: Unifying Programmatic Advertising and Recommender Systems

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Retailing and media platforms recommend two types of items to their users: sponsored items that generate ad revenue and non-sponsored ones that do not. The platform selects sponsored items to maximize ad revenue, often through programmatic auctions, and non-sponsored items to maximize user utility with a recommender system (RS). We develop a binary integer programming model to allocate sponsored recommendations considering dual

objectives of maximizing ad revenue and user utility. We propose an algorithm to solve it in a computationally efficient way. Our method is a form of postfiltering to a traditional RS, making it widely applicable in two-sided markets. We apply the algorithm to data from an online grocery retailer and show that user utility for the recommended items can be improved while reducing ad revenue by a small amount. This multiobjective approach unifies programmatic advertising and RS and opens a new frontier for advertising and RS research. We provide an extended discussion of future research topics.

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Two-sided markets are defined as intermediary platforms that enable direct interactions between two distinct stakeholder groups, generically labeled *consumers* and *providers* (Hagiu and Wright 2015). The media have long been held up as an exemplar. Media companies attract an audience of consumers with, for example, news or entertainment content (e.g., a TV program or magazine) and then sell advertisers access to the audience. Just as advertisers pay media companies for access to their audiences, they pay platforms for access to consumers. The two stakeholder groups here are consumers and advertisers. In recent years, a wide variety of different types of two-sided markets have been introduced, often under the name *platform*. Platforms can, therefore, be viewed as a new form of media. For example, retail-based shopping platforms like Taobao in China and Amazon Marketplace in the United States match consumers with

retailers. The platform attracts consumers and matches them with retail providers through recommendations. Instead of consumers, the terms *consumer* and *user* are often used; we employ *user* to refer to the first stakeholder group.

Platforms can show two types of recommendations, *sponsored* and *nonsponsored*, where sponsored providers (i.e., advertisers) pay the platform for access to the user and nonsponsored providers do not. Sponsored recommendations are often sold on programmatic auctions where the platform can adopt various strategies to sell slots (Sayedi 2018; Malthouse, Maslowska, and Franks 2018) to the highest bidder. Because nonsponsored recommendations do not generate ad revenue, we assume that platforms select nonsponsored items to be relevant to the user, which is often done using a class of machine learning and artificial intelligence (AI) algorithms known as *recommender systems* (RS), defined as “[s]oftware tools and techniques providing suggestions for items to be of use to a user” (Ricci, Rokach, and Shapira 2015, p. 1). One notable feature of this RS definition is its exclusive focus on a single stakeholder: the user. The sole purpose of a traditional RS is to recommend items that maximize the user’s utility.

While most traditional RS generate recommendations to maximize the utility for the end user, this article develops algorithms for more complex systems where there is another stakeholder—the advertiser—and another objective created by the possibility of generating ad revenue through sponsored recommendations. For example, consider a user looking for a pasta sauce on an online grocer’s website. A traditional RS would recommend pasta sauces (items) to maximize the user’s utility, but what if some advertisers were willing to pay the retailer to be recommended? In this case the retailer has a second, competing objective of earning revenue from the advertiser. The situation we described is an example of a multiobjective, multistakeholder RS, abbreviated as MRS (Burke and Abdollahpouri 2017). This is a new and important problem in both advertising and RS that has received little attention in the literature. The MRS must decide which advertisers to recommend while striking a balance between sponsored and nonsponsored recommendations. We develop the MRS specifically for the sponsored recommendation problem, where a platform must decide which personalized set of providers to recommend to each user. We express the combined objectives in a single equation:

$$Q = \gamma(\text{user utility}) + (1 - \gamma)(\text{ad revenue}), \quad (1)$$

where  $\gamma$  is a parameter that determines how much weight to give to each of the two objectives and  $Q$  is the objective function value to be maximized. A platform that allocates sponsored recommendations with an auction has

$\gamma = 0$  and is maximizing ad revenue. An RS that considers only the user’s utility, such as those used to allocate nonsponsored recommendations, has  $\gamma = 1$ . Rather than focusing on one or the other, this equation allows for a continuum between the two competing objectives, providing the platform manager a way to manage the trade-off between the two objectives.

We formulate a postprocessing integer programming model to maximize the dual-objective function in Equation (1) over all users, subject to constraints that the advertiser has budget to pay and the number of sponsored recommendations to the user has not exceeded an analyst-specified threshold. We show how to solve the optimization problem in a computationally efficient way and illustrate the approach using real data from an online grocery retailer. Our approach improves user utility substantially while decreasing ad revenue by a small amount. This work follows a design-oriented research approach that has commonly been used in technical and computer sciences (Verschuren and Hartog 2005) and has, due to the nature of the field, recently been gaining traction in advertising research (see Henseler 2017). With this article, we advance research on programmatic advertising and RS by developing algorithms for more complex systems where there is another stakeholder (i.e., the advertiser), and another objective (i.e., generating ad revenue through sponsored recommendations).

## LITERATURE REVIEW

Our approach postulates that there are two types of recommendations, sponsored and nonsponsored, which are selected with different objectives. This section begins with a review of how ad space for sponsored content and display ads is sold, and then gives an overview of the RS used to recommend nonsponsored content. We then discuss existing literature on how to manage competing objectives.

### Programmatic Auctions Maximizing Ad Revenue to Platforms

Search and display advertising is often sold using programmatic auctions. An auction is held for an impression, and different advertisers place bids. Typically, the auctions are second price, where the winner pays the second-highest bid amount for the space. The second-price auctions have an optimal strategy for an advertiser of bidding the expected value of the impression (see Edelman, Ostrovsky, and Schwarz 2007). There is a rich literature within computer science and marketing on bidding strategies. For example, Perlich et al. (2012) presented a bid-optimization approach that combines several supervised

learning algorithms, as well as second-price auction theory, to determine the correct price and ensure that the right message is delivered to the right person at the right time. Wu et al. (2015) proposed a way to leverage machine learning to predict the winning amount from the bidding history. It is important to note that in these strategies the platform is accepting the best bid and is therefore maximizing only its ad revenue. The platform does not consider the user’s utility when it awards exposure to an advertiser.

Our formulation of the MRS problem for sponsored recommendations is related to the AdWords problem (Leskovec, Rajaraman, and Ullman 2014, section 8.4.2), which considers “online” situations where user queries come in over time to some system and assumes (1) a set of bids from advertisers for a query; (2) known (or predicted) click-through rates (CTRs) for each advertiser–query pair; (3) a budget for each advertiser; and (4) an upper bound for the number of ads to be displayed with each query. Algorithms solving the problem return search results that do not exceed the upper bound, and the advertisers have both bid on the search term and have budget to pay if the ad is clicked on.

### Recommendation Systems Maximizing User Utility

RS is a well-established branch of machine learning and AI. Ekstrand, Riedl, and Konstan (2011) give an overview of their history and survey different collaborative filtering approaches; Adomavicius and Tuzhilin (2005) is a highly cited survey of the field; and Ricci, Rokach, and Shapira (2015) is an extensive collection from contributors covering the different state-of-the-art areas of RS. An RS incorporates a set of users and a set of items. The core task is to generate personalized matches between users with items that are of interest to them. We denote the set of users by  $\mathcal{U} = \{1, \dots, m\}$  and the set of items by  $\mathcal{I} = \{1, \dots, n\}$ . We reserve the variable  $u$  to index users and  $i$  to index items.

The starting point of data for a RS is the  $m \times n$  rating matrix  $\mathbf{R}$ , where element  $r_{ui}$  is the “rating” of item  $i$  by user  $u$ . The term *rating* denotes preference or utility. A rating could be *explicit*, such as a rating on a five-point scale of how much the user liked an item (e.g., a movie, song, restaurant). In our situation we are more likely to have what the RS literature calls *implicit ratings*, which are given by whether or not the user has purchased an item, or the number of times an item is purchased or consumed.

RS usually have two possible goals: *prediction* and *recommendation*. The prediction goal is to estimate the missing ratings (denoted by  $\hat{r}_{ui}$ ). The recommendation goal is to recommend  $k$  items to some user, which is called a

top- $k$  list. For example, a retailer might send a personalized e-mail with a  $4 \times 5$  grid of item suggestions, which is called a “top-20” list. If the goal is to recommend a list of  $k$  items to maximize the utility of end users, we can choose the  $k$  items with the highest estimated utility  $\hat{r}_{ui}$  for each user, although there could be other considerations, such as recommending items from a diverse set of product categories. Many algorithms have been proposed to compute estimates  $\hat{r}_{ui}$ . We briefly summarize one specific RS algorithm, user-based collaborative filtering (UBCF). Suppose that the RS must make a prediction  $\hat{r}_{ui}$  for target item  $i$  by some active user  $u$ , where  $u$  has not rated  $i$ . UBCF first finds other users whose ratings are similar to the active user and who have rated  $i$ . These other users are called *nearest neighbors*. Prediction  $\hat{r}_{ui}$  is then the average of the nearest neighbors’ ratings of item  $i$ . Additional refinements will improve the estimate, such as giving more weight to the ratings of item  $i$  of neighbors who are more similar to active user  $u$ . While validating our proposed algorithm on online grocery data, we use UBCF to calculate user utility.

### Multistakeholder Recommender System

MRS refers to a design that incorporates the interests of other parties (Burke et al. 2016; Abdollahpouri, Burke, and Mobasher 2017; Abdollahpouri et al. 2019). The objectives of different stakeholders, however, may conflict (Ribeiro et al. 2012; Sürer, Burke, and Malthouse 2018). For example, in the case of a two-sided retail platform, the objective for users is to find items that maximize their utility, while the objective for a specific retail provider is to maximize its orders, which are stimulated by being recommended to many users. The platform also wants to generate ad revenue. Managing recommendations for a platform is therefore a complex task. However, previous studies have shown that RS that consider profits can have a positive effect on purchasing without diminishing trust (Panniello, Hill, and Gorgoglione 2016). Similarly, Azaria et al. (2013) also demonstrate that an RS can increase revenue without a significant drop in user satisfaction.

While Burke et al. (2016) conceptualized the MRS problem, to the best of our knowledge there is no known general solution. As MRSs have a wide variety of forms (see Burke and Abdollahpouri 2017), they require a variety of solution approaches. In our situation the two main stakeholders are users and advertisers. Users expect recommendations to match their preferences and to maximize their utility. Advertisers want to sell their items. The platform wants users to return while also earning ad revenue.



TABLE 1  
Selected Literature on Multiobjective, Multistakeholder Recommender Systems (MRS)

Literature	Context	MRS	Algorithm	Objective
Rodriguez, Posse, and Zhang (2012)	Job posting	Multiobjective	RS using semantic matching and extraneous factors	User utility with extraneous factors
Ribeiro et al. (2012)	Movies and music	Multiobjective	Strength Pareto approach in hybrid RS	Accuracy, novelty, and diversity
Burke et al. (2016)	Movies	Yes	Greedy approach	Multidimensional utility
Sürer, Burke, and Malthouse (2018)	Movies and retailing	Yes	Constraint-based integer programming optimization model	Utility of buyers and providers
Ben-Porat and Tennenholtz (2018)	Conceptual	Yes	Game theory and Shapley mediator	Fairness and stability
This article	Sponsored recommendations in programmatic advertising	Yes	Postfiltering optimization RS	User utility and ad revenue

Note. RS = recommender systems.

Previous studies have also explored multiobjective (see Rodriguez, Posse, and Zhang 2012; Ribeiro et al. 2012) and multicriteria (see Adomavicius and Tuzhilin 2011; Zheng 2017) RS. However, they do not address the specific problems with sponsored ads. For example, Ribeiro et al. (2012) use the strength Pareto approach to optimize three different objectives of accuracy, novelty, and diversity. Further, Zheng (2017) maximizes performance in multicriteria RS. Relatedly, other authors have explored the greedy approach (Burke et al. 2016), probabilistic topic models (Zihayat et al. 2019), and the Shapley mediator using game theory (Ben-Porat and Tennenholtz 2018) to optimize user utility functions. From the limited literature on MRS (Table 1), one of the first attempts to propose a model for the MRS problem is Sürer, Burke, and Malthouse (2018), which focused specifically on retail platforms and the problem of promoting retailer retention by guaranteeing a minimum level of exposure to each but did not consider advertising. This study proposes a post-processing step for use after a traditional RS has estimated the utilities of each user for each item.

#### THE MULTISTAKEHOLDER SPONSORED ADVERTISING RECOMMENDATION ALGORITHM

We assume that the platform must generate  $k$  recommendations for each user, which is called a top- $k$  list in the RS literature. For example, the platform may have to generate e-mail newsletters or promotions for its user, each containing  $k$  recommended items. Or a retailer may

send out shipping list e-mails to users placing an order today, and at the bottom of the e-mail it recommends  $k$  items, attempting to stimulate another order. Some items are sponsored, where each provider has some fixed ad budget for the period, and other items are not sponsored. To avoid showing too many sponsored items to any single user, we also allow for the platform to specify a constraint restricting the maximum number of sponsored items.

We assume that a platform has  $n$  items that can be recommended, some of which are sponsored. Our task is to identify personalized top- $k$  lists for each of  $m$  users. Among the  $k$  items, at most  $s_{\max} \leq k$  can be sponsored, which allows for the platform to set an upper limit on the amount of advertising to any single user if it wishes. For now, we assume that the  $m$  users are known in advance. Let  $a_{ui}$  be the ad revenue (or expected revenue, as is discussed next) associated with displaying item  $i$  to user  $u$ . If item  $i$  is not sponsored, then  $a_{ui} = 0$ . Let  $\beta_i$  be the total advertising budget associated with item  $i$ , where nonsponsored items have  $\beta_i = 0$ .

We model the recommendation output via decision variable  $x_{ui}$  where  $x_{ui} = 1$  if item  $i$  is included in the top- $k$  list for user  $u$  and 0 if not. The  $m \times n$  matrix of  $x_{ui}$  variables, denoted in matrix form as  $\mathbf{X}$ , determines which recommendations will be shown. Since each user receives  $k$  recommendations, exactly  $k$  values of  $x_{ui}$  will equal 1 for a given user. We propose the following optimization model, where  $\forall$  means “for all” and  $\in$  means “element of”:

$$\max_{\mathbf{X}} \left[ \underbrace{\gamma \sum_{u \in \mathcal{U}} \sum_{i \in \mathcal{I}} \hat{r}_{ui} x_{ui}}_{\text{User utility}} + (1-\gamma) \underbrace{\sum_{u \in \mathcal{U}} \sum_{i \in \mathcal{I}} a_{ui} x_{ui}}_{\text{Ad revenue}} \right] \quad (2)$$

subject to:

$$\sum_{i \in \mathcal{I}} x_{ui} = k \quad \forall u \in \mathcal{U} \quad (3)$$

$$x_{ui} \in \{0, 1\} \quad \forall i \in \mathcal{I}, u \in \mathcal{U} \quad (4)$$

$$\sum_{i \in \mathcal{I}} 1(a_{ui} x_{ui} > 0) \leq s_{\max} \quad \forall u \in \mathcal{U} \quad (5)$$

$$\sum_{u \in \mathcal{U}} a_{ui} x_{ui} \leq \beta_i \quad \forall i \in \mathcal{I} \quad (6)$$

We now discuss each part of the model, starting with the objective function in Equation (2). The optimization problem is to select from all possible  $\mathbf{X}$  values, in other words, the top- $k$  lists for the  $m$  users, the values of  $\mathbf{X}$  to maximize a two-part objective. The first part, labeled “user utility,” measures the total utility of the items recommended to all users. Product  $\hat{r}_{ui} x_{ui}$  equals 0 for all items not selected, and the estimated utility for those selected; terms are summed over all users and items. The second part of the objective function, labeled “ad revenue,” measures the total revenue from recommended sponsored items. Product  $a_{ui} x_{ui}$  equals 0 for nonrecommended items and  $a_{ui}$  for recommended ones. The analyst-specified tuning parameter  $\gamma$  ( $0 < \gamma \leq 1$ ) determines how much weight to assign to the two parts. When  $\gamma = 1$  the objective gives all weight to user utility and produces the same solution as a traditional RS. When  $\gamma \approx 0$  the algorithm places nearly all the weight<sup>1</sup> on ad revenue and mostly ignores user utility, which is how programmatic advertising auctions operate. The constraints are interpreted as follows:

- Equation (3): The number of recommended items is  $k$  for each user  $u$ .
- Equation (4):  $x_{ui}$  equals 0 or 1, making this a binary integer programming problem.
- Equation (5): The number<sup>2</sup> of sponsored recommendations shown to user  $u$  must not exceed  $s_{\max}$ , which is specified by the analyst. Note that  $1(\cdot)$  is the indicator function, which equals 1 when the Boolean condition in the argument is satisfied and 0 otherwise.
- Equation (6): Total ad revenue from item  $i$  does not exceed the budget for that item,  $\beta_i$ .

## Discussion of the Model

We discuss the two parts of the objective function (2): total user utility and total ad revenue. Figure 1 shows expected curves for the two parts as a function of  $\gamma$ . First,

suppose that  $\gamma \approx 0$ , indicating that the algorithm should focus on optimizing ad revenue. The amounts of user utility and ad revenue are indicated by the black dots on the left side ( $\gamma \approx 0$ ) of the respective plots. Ad revenue is at its maximum value, while user utility is at its smallest value, although sponsored recommendations should produce positive user utility. If we start to consider user utility by increasing the value of  $\gamma$ , two things will happen: (1) user utility will either increase or stay the same, and (2) ad revenue will either decrease or stay the same. The best results for the proposed algorithm will be achieved when both the the user utility (left) and ad revenue (right) curves are concave, shown by black, solid lines. In this case, a small increase of  $\gamma$  from 0 produces a large increase in user utility (left) with very little loss in ad revenue (right). The worst case is when both curves are convex, shown by red, dashed lines, where a small increase of  $\gamma$  from 0 results in a large decrease in ad revenue with little improvement to user utility.

Starting at the right side of the plot at the red triangle points, where  $\gamma = 1$ , indicates that the algorithm should focus exclusively on user utility, as with a traditional RS. At this point, user utility is maximized, while ad revenue is at its lowest point. The same conclusions hold that the concave functions are the best scenario and convex the worst. If we decrease  $\gamma$  (allocating some weight to ad revenue) and if the curves are concave, then utility decreases by a small amount (left) while ad revenue increases substantially (right). The curvature will be investigated in our empirical examples for real data.

The curves will be concave when there are many sponsored and nonsponsored items with roughly the same user utility, so that the platform can substitute one item for another in a top- $k$  list without sacrificing much user utility. Likewise, when there are many sponsored items with roughly the same ad revenue, substitutions can be made to improve user utility.

## Solving the Optimization Problem

To solve the optimization problem, we rewrite the objective function (2):

$$\begin{aligned} & \left[ \underbrace{\gamma \sum_{u \in \mathcal{U}} \sum_{i \in \mathcal{I}} \hat{r}_{ui} x_{ui}}_{\text{User utility}} + (1-\gamma) \underbrace{\sum_{u \in \mathcal{U}} \sum_{i \in \mathcal{I}} a_{ui} x_{ui}}_{\text{Ad revenue}} \right] \\ & = \sum_{u \in \mathcal{U}} \sum_{i \in \mathcal{I}} x_{ui} \underbrace{(\gamma \hat{r}_{ui} + (1-\gamma) a_{ui})}_{c_{ui}} \end{aligned}$$

where optimization criterion  $c_{ui} = \gamma \hat{r}_{ui} + (1-\gamma) a_{ui}$ . Clearly this expression is maximized by selecting the largest  $c_{ui}$  values, subject to the constraints. This leads to the algorithm in Table 2. The most computationally

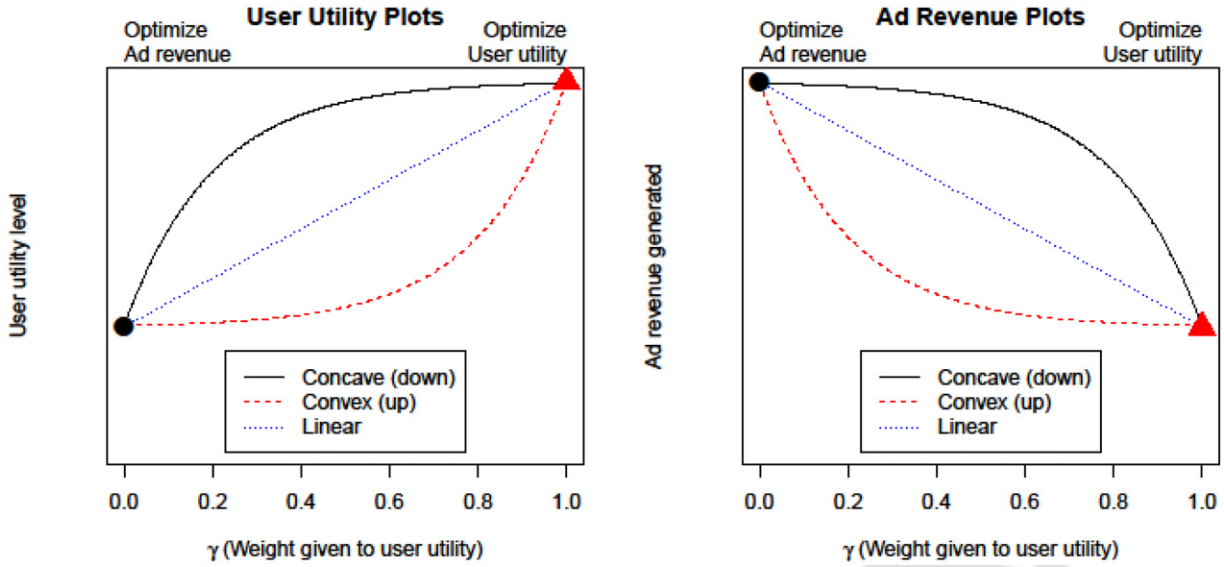


FIG. 1. Hypothetical user utility and ad revenue curves.

TABLE 2

Algorithm 1: The Multistakeholder Advertising Recommendation Algorithm

Require: (1) Analyst sets (1)  $\gamma$ , the weight for user utility, and (2)  $s_{\max}$ , the max number sponsored recommendations shown to a user. Advertiser sets budget  $\beta_i$ .

$$c_{ui} \leftarrow \gamma \hat{r}_{ui} + (1 - \gamma)a_{ui}, \quad \forall u, i$$

Sort  $c_{ui}$  in descending order with index function mapping counting numbers  $h \in \{1, \dots, mn\}$  to user-item pairs

$$(u(h), i(h)) \text{ such that } c_{u(1), i(1)} \geq c_{u(2), i(2)} \geq \dots \geq c_{u(mn), i(mn)}.$$

$$s_u \leftarrow 0, \quad \forall u$$

$$b_i \leftarrow 0, \quad \forall i$$

$$x_{ui} \leftarrow 0, \quad \forall u, i$$

$$k_u \leftarrow 0, \quad \forall u$$

Initialize counter of sponsored ads to user  $u$

Initialize spent ad  $i$  budget item  $i$

Initialize item to be not selected

Initialize number recommended to user  $u$

**for**  $h \leftarrow 1$  until all users are assigned exactly  $k$  items **do**

**if**  $k_{u(h)} < k$  **then**

$$x_{u(h), i(h)} \leftarrow 1$$

$$k_{u(h)} \leftarrow k_{u(h)} + 1$$

**if**  $a_{u(h), i(h)} > 0$  and  $b_{i(h)} + a_{u(h), i(h)} \leq \beta_{i(h)}$  and  $s_{u(h)} < s_{\max}$  **then**

Label item sponsored

$$s_{u(h)} \leftarrow s_{u(h)} + 1$$

$$b_{i(h)} \leftarrow b_{i(h)} + a_{u(h), i(h)}$$

**end if**

**end if**

Add item to top- $k$  list

Increment recommendation count

Increment sponsored count

Tally ad spend

**end for**

expensive part of the algorithm is sorting the  $mn$  elements of  $c_{ui}$  in descending order. This sorting has superlinear computational complexity, requiring on the order of

$mn \log(mn)$  operations, so this algorithm will be computationally feasible for very large problems. Sorting is indicated by an index function that returns a user-item pair,



for example, no other  $c$  value is larger than  $c_{u(1),i(1)}$ , and  $c_{u(h),i(h)}$  gives the  $h^{\text{th}}$  largest  $c$  value. The variable  $s_u$  counts the number of sponsored recommendations shown to user  $u$ ,  $b_i$  totals the amount of ad budget from item  $i$  spent, and  $k_u$  counts the number of items recommended to user  $u$ . The algorithm walks through  $c_{ui}$  one element at a time, starting from largest, until each of the  $m$  users has received  $k$  recommendations.

We close this section by discussing situations that are potentially challenging and how we address them in the algorithm. First, there could be situations during the execution of the algorithm in line 11 where a sponsored item ( $a_i > 0$ ) has the highest user utility (i.e., higher than remaining nonsponsored items), but either the ad budget ( $\beta_i$ ) for the item has been exhausted or the maximum number of sponsored item slots ( $s_{\max}$ ) has been filled. In these cases, the algorithm should display the item as nonsponsored because it has the highest user utility. To have transparency, there should not be a sponsored designation displayed next to the item, and the retailer should not charge for the recommendation.

Second, for  $\gamma < 1$  the sort order of  $c_{ui}$  changes if ad revenue is set to 0. An item has more value to the platform when it is sponsored than when it is not, in other words  $\gamma\hat{r}_{ui} + (1-\gamma)a_{ui} > \gamma\hat{r}_{ui}$ . An easy way to handle this is to include all sponsored items twice in the list, once as sponsored and once as nonsponsored ( $a_{ui} = 0$ ), and then do the sort. Therefore, if an item has already been selected to be shown as sponsored, it cannot also be selected as nonsponsored. Last, when allocating the last ( $k^{\text{th}}$ ) slot, there could be multiple items with the same value of criterion  $c_{ui}$ . When the criterion values are tied it does not matter which one is selected, and the algorithm could select one at random or with another tie-breaking rule (see Bryce and Colbourn 2007).

Third, one of the most common RS problems is the item cold-start, where there are new items. Because a new item has no ratings, UBCF will never display it and older items will dominate the recommendations. Our proposed algorithm is a postprocessing procedure to the aforementioned step, and a retailer should have an existing method for dealing with cold-start, such as a hybrid RS combining content-based RS (which use meta data about items instead of ratings from other users) for new items with UBCF. Our algorithm could then be deployed separately on each of the component RS.

### Commensurate Units

The analyst should be aware that the two parts of the objective function have different units:  $a_{ui}$  is likely measured in a currency such as dollars or euros, while the units for  $\hat{r}_{ui}$  depend on how user utility is operationalized.

For example, it could be the log number of previous purchases plus one, the probability of purchase, or the estimated rating on a five-point scale from 1 to 5. One way to address this problem is to use “unitless,” standardized versions of  $a_{ui}$  and  $\hat{r}_{ui}$  in the objective function.

A more desirable common unit would be to express  $\hat{r}_{ui}$  in the same monetary unit as  $a_{ui}$ , for example, dollars. Estimating the monetary value, however, is a complex task requiring substantial modeling. In addition to quantifying the probability of a current purchase, one would also have to consider the long-term implications. If a recommended item produces a sale, the retailer receives some short-term profit from selling the item but also has a user with better recency-frequency-monetary (RFM) status: Recency is now zero days, frequency value is one larger, and monetary value is greater (Malthouse, Maslowska, and Franks 2010). All three variables tend to be associated with higher purchase probabilities in the future (Blattberg, Malthouse, and Neslin 2009). Failing to account for the long-term effects produces evaluations of the value of the recommendation that are biased downward. As we discuss in the future research section, if such common units are available, one could optimize over  $\gamma$  as a decision variable rather than specifying it exogenously.

### Ad Revenue

Our proposed algorithm requires the analyst to provide values of  $a_{ui}$ , the ad revenue associated with item  $i$  for user  $u$ . Notice that there are two subscripts, allowing different revenue amounts for different users and items. This section discusses the source of the  $a_{ui}$  values. We intend for our algorithm to be general and to work for many current RS as well as future ones. We assume that advertisers can set an ad budget and that there are auctions for exposures. The advertiser can select items on which to place bids and may have the ability to modify the bid amount based on additional information about the user; for example, the advertiser could increase the bid for users in a certain demographic segment.

There are currently different revenue models for programmatic advertising. For example, advertisers can pay for a view, click, lead, conversion, or engagement, such as signing up for an e-mail list or newsletter. These models have corresponding metrics such as cost per view (CPV, also known as CPM), cost per click (CPC), etc. The simplest case is when the fixed cost per exposure and the value  $a_{ui}$  is a constant. In more complicated cases,  $a_{ui}$  is an expected amount, which may be computed from a predictive machine learning model or various auction strategies. For example, there could be a model estimating the chance of a conversion and probability of winning the



755 auction based on a certain bid. However, we focus on the  
756 algorithm and take ad revenue as a given.

## 757 EMPIRICAL EVALUATION

759 We first show an idealized example of our empirical  
760 evaluation to clarify the two competing objectives of our  
761 study: user utility and ad revenue. Next, we use data  
762 from an online grocery retailer to study the trade-off  
763 between the two.

### 764 Motivating Example

765 Suppose that advertiser  $A$  places the highest bid for a  
766 sponsored recommendation to a user. Advertiser  $B$  places  
767 a bid that is only slightly less than  $A$ 's but would provide  
768 the user substantially more utility than  $A$ . We argue that  
769 the platform should consider giving the slot to  $B$  even  
770 though it would generate less ad revenue. A possible  
771 financial justification for this decision is that  $B$  may gener-  
772 ate higher lifetime value, where the user buys  $B$ , ultim-  
773 ately is satisfied with  $B$ , and buys again from the  
774 platform in the future. If the platform had shown  $A$ , then  
775 either the user would not buy it or would not be satisfied  
776 and would be less likely to return to the platform in the  
777 future. An alternative scenario is also conceivable, where  
778 the ad revenue from  $B$  is substantially lower and/or  $B$   
779 provides no advantage over  $A$  in user utility. In this scen-  
780 ario the platform should display  $A$ . In this section, we  
781 evaluate these issues empirically. We demonstrate the  
782 feasibility of our algorithm and investigate the sensitivity  
783 of the ad revenue and user utility curves as a function of  
784  $\gamma$  using data from an online grocery retailer.

### 785 Data and Preparation

786 The data are from an online grocery retailer in the  
787 United States operating in 12 states and Washington DC,  
788 with approximately 25,550 unique stock-keeping units  
789 (SKUs), 99,556 unique users, and 2,286,831 orders. The  
790 first step in building an RS is to define what an "item" is  
791 by aggregating the SKUs, as each size, flavor, and so on  
792 has its own SKU. For example, in the subcategory  
793 "soda," the brand "Diet Coke" is separate from "Coke  
794 Classic." The retailer provided a taxonomy of 136 subca-  
795 tegories, which, when crossed with brand names, gives  
796 3,966 combinations. We clean the data further by combin-  
797 ing different brand lines of the same product into a  
798 single brand. For example, within diapers Pampers is a  
799 single brand, while Huggies has many subbrands such as  
800 Little Movers, OverNites, and Pull-Ups, which are col-  
801 lapsed into one Huggies brand. We count the number of  
802 orders that contain each subcategory-brand combination.

803 With this approach, the brand "Dean's" in the ice cream  
804 subcategory is a distinct brand from Dean's milk, Dean's  
805 juice and Dean's cottage cheese, but all flavors and sizes  
806 of Dean's ice cream are grouped together. Many brand-  
807 subcategory combinations have small order counts. For  
808 the purpose of this example, we minimize rare items by  
809 relabeling any subcategory-brand combination with fewer  
810 than 2,500 orders as having brand "other," which gives a  
811 total of  $n = 1,021$  combinations, defining an "item" for  
812 the algorithm.

813 We examine only regular users who have placed 15 or  
814 more orders and have purchased within the past six  
815 months (i.e., recency  $\leq 0.5$  years), giving a universe of  
816 19,360 users. For the purpose of this example, we draw a  
817 simple random sample of size  $m = 2,000$  users and build  
818 our  $\mathbf{R}$  matrix with roughly 2 million entries (2,000 users  
819  $\times$  1,021 items). We use implicit ratings by taking the log  
820 number of past purchases, which provides gradation  
821 between products that are never purchased, purchased  
822 occasionally, and purchased often by a user.

823 In the current data set, items were not sponsored. To  
824 study sponsored items, we assume that some fraction of  
825 the branded items is sponsored. Private-label items are not  
826 allowed to be sponsored because they are owned by the  
827 retailer. Likewise, we exclude "other" subcategories, for  
828 example, "other cottage cheese," because they would be  
829 composed of multiple small brands. We assign a \$1,000  
830 budget to each branded item for sponsored recommenda-  
831 tions and assume advertising revenue ( $a_i$ ) drawn randomly  
832 from the Gaussian distribution  $\mathcal{N}(\mu = 1, \sigma = 0.2)$ . The  
833 algorithm is then executed, and the results are compared  
834 for different values of  $\gamma$ . We conduct robustness checks by  
835 varying the fraction of sponsored items.

### 836 Preprocessing Step: Generating User Utility Using 837 Traditional RS

838 Our proposed algorithm post processes ratings from a  
839 traditional RS to address the MRS problem. Hence, an  
840 RS must first generate ratings for products each user has  
841 not rated yet. For this example, we compare item- and  
842 user-based collaborative filtering (IBCF and UBCF). For  
843 UBCF, we use cosine similarity<sup>3</sup> and vary the number of  
844 nearest neighbors (NNs): 5, 10, 20, 30, 50, 70, 90, 100,  
845 and 110. The performance of both traditional RS is meas-  
846 ured by the root mean square error,

$$847 \text{RMSE} = \sqrt{\frac{1}{|T|} \sum_{(u,i) \in T} (\hat{r}_{ui} - r_{ui})^2},$$

848 where  $T$  is the test set and  $|T|$  is its cardinality. We use  
849 fivefold cross validation to evaluate traditional RS algo-  
850 rithms and follow the established model-building process  
851 outlined in Ekstrand, Riedl, and Konstan (2011, section  
852 853 854 855 856 857 858 859 860 861 862

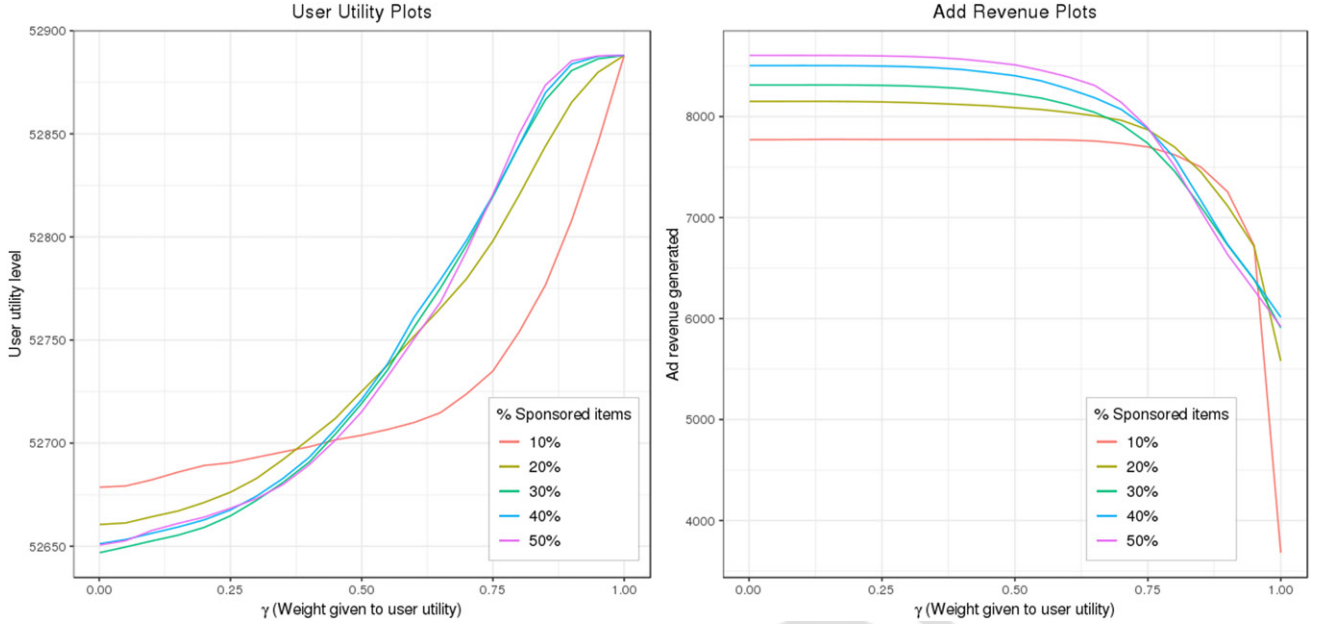


FIG. 2. User utility and ad revenue curves estimated for real data from an online grocery retailer.

TABLE 3  
Results from Traditional RS: Item-Based and User-Based Collaborative Filtering (IBCF and UBCF)

Algorithm	NNs	RMSE
UBCF	5	0.672
	10	0.666
	20	0.661
	30	0.657
	50	0.652
	70	0.648
	90	0.646
	100	0.645
IBCF	110	0.644
	—	0.965

*Note.* Two traditional RS (IBCF and UBCF) are used to generate user ratings and are evaluated using root measure square error (RMSE). UBCF was run for multiple nearest neighbors (NNs). Output matrix of traditional recommender systems is input to our proposed algorithm.

3.2) and Breese, Heckerman, and Kadie (1998). Table 3 summarizes the results of evaluation for traditional RS. The UBCF model performs better on our test data set than IBCF. There is very little difference in RMSE between different numbers of nearest neighbors, and we use 30.

### Results from Proposed Algorithm

After estimating the ratings with UBCF, we test our algorithm. The goal is to recommend the top-20 items

( $k_u = 20$ ) to each user, among which at most three ( $s_{\max} \leq 3$ ) can be sponsored. To put both ratings ( $\hat{r}_{ui}$ ) and ad revenue ( $a_{ui}$ ) values on the same scale, we use their  $z$  scores to calculate  $c_{ui}$ . We expect that a small increase of  $\gamma$  from 0 will produce a large increase in user utility with very little loss in ad revenue (this is the best condition for our proposed algorithm, as mentioned before). Figure 2 displays the results of the algorithm for user utility and ad revenue as a function of  $\gamma$  with different percentages (10%, 20%, 30%, 40%, 50%) of sponsored items. In all five cases, we see that as  $\gamma$  (the weight given to user utility) increases from 0 to 1, user utility increases, and ad revenue decreases monotonically. The ad revenue plot (right) is mostly concave, as we had hoped. The utility curve (left), however, is convex for small values of  $\gamma$ , but mostly concave for large values.

In the case of  $\gamma \approx 0$ , all weight is given to optimizing ad revenue, which maximizes ad revenue and minimizes user utility. This can be considered the status quo for sponsored ads. As shown in ad revenue plot (Figure 2), when the number of sponsored items increase, there are more options to choose from and ad revenue grows. In the user utility plot, having fewer options in sponsored items would lead the algorithm to choose items with higher user utility, generating higher overall user utility in the case of 10%, compared to 50% of sponsored items.

After  $\gamma$  reaches approximately 0.5, the ad revenue plots show a faster decrease in the cases with higher number of sponsored items. With more sponsored items in the inventory, as  $\gamma$  increases,  $c_{ui}$  puts more weight on user utility and the algorithm has more ways to select sponsored 970

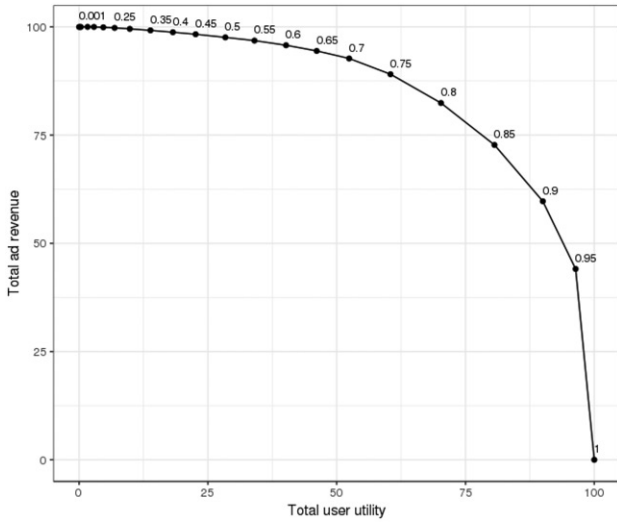


FIG. 3. Plot showing total ad revenue against the total user utility for different values of  $\gamma$ .

items that have lower ad revenue but higher ratings. At the end, the sum of ad revenue has a faster decline in the cases with more sponsored items as to when the number of sponsored items is limited, since those limited items might have had higher ad revenue with higher ratings. In all cases, the ideal scenario with both curves concave is partially realized.

#### Comparison with Traditional RS (UBCF)

We compare our proposed algorithm for MRS with traditional RS, in other words, UBCF. While evaluating MRS, previous studies have shown that a slight decrease in one objective improves over the previous system if there is a substantial increase in competing objectives (Burke et al. 2016; Rodriguez, Posse, and Zhang 2012). To evaluate the performance of our algorithm in comparison with traditional RS, we show the change in one objective as we vary the weight given to the competing objective. Recall when  $\gamma = 1$ , the algorithm chooses the top 20 items solely based on user's utility. At 20% sponsored items, we observe that as  $\gamma$  changes from 1 to 0.75, user utility decreases by only 0.17%, while ad revenue increases substantially by more than 40% (see Figure 2).

#### Evaluation of Proposed Algorithm

We evaluate our algorithm by plotting the total ad revenue against the total user utility for different values of  $\gamma$ , as shown in Figure 3. For comparison, the axes have been scaled so that 0 indicates the minimum value of ad revenue or utility and 100 indicates the maximum value. The values of the points on the curve correspond to different  $\gamma$  values. This curve resembles a receiver operator

curve (ROC; e.g., Fawcett 2006), where, in this application, the area under the curve (AUC) measures how much flexibility the platform has. In an ideal situation, the platform would be able to achieve 100% of both the ad revenue and user utility, giving a point in the upper right corner of the graph. In our example, we can see that reducing the ad revenue by a fairly small amount increases user utility substantially. For example, changing  $\gamma$  from 0 to 0.50 achieves roughly 28 points' increase in user utility while ad revenue decreases by only 2 points.

We have also measured the ranking performance of our proposed algorithm by calculating the normalized discounted cumulative gain ( $nDCG$ ) for all the values of  $\gamma$  with different percentages of sponsored items. It is one of the most popular rank-based metrics used in RS. This metric aims to capture the quality of a particular ranked list by assuming that an RS is more efficient if the higher rated items appear early in the recommendation list. In this case, the evaluated ranked list is the top- $k$  recommended items to each user.  $nDCG$  varies between zero and one, and is defined as

$$nDCG = \frac{DCG}{IDCG}$$

$$DCG = \frac{1}{m} \sum_{u=1}^m \left( \hat{r}_{u1} + \sum_{i=2}^k \frac{\hat{r}_{ui}}{\log_2(i+1)} \right)$$

$nDCG$  evaluates an ideal ranked list ( $IDCG$ ) against the ranked list generated by our proposed algorithm. Here,  $IDCG$  is the  $DCG$  of top- $k$  items for each user, chosen solely based on user utility, which is the list generated by the traditional RS, UBCF. The perfect ranking would have  $nDCG$  of value 1.

Table 4 shows the evaluation results of our proposed algorithm in terms of  $nDCG$  for different percentages of sponsored items. When  $\gamma = 1$ , the algorithm chooses the top-20 items exclusively based on user's utility, so  $nDCG$  is at its maximum. As  $\gamma$  decreases, more weight is given to improving the ad revenue, but as we can observe from the results, it does not hurt the overall quality of the recommendations by much.

#### DISCUSSION

This study shows how platform managers can consider both ad revenue and user utility while recommending sponsored items to the users. This represents a paradigm shift from extant programmatic advertising approaches that focus on maximizing ad revenue and consider user utility only through click probabilities. The approach described in this article treats the problem of MRS in platform settings as a postprocessing optimization step to be applied after user utilities have been estimated by a traditional RS. Thus, our approach is not dependent on any particular RS



TABLE 4  
Evaluation of Recommendation Ranking Produced by the Proposed Algorithm for Different Percentages of Sponsored Items, Measured in  $nDCG$

$\gamma$	$nDCG$ 10%	$nDCG$ 20%	$nDCG$ 30%	$nDCG$ 40%	$nDCG$ 50%
0.001	0.977	0.975	0.975	0.975	0.975
0.1	0.977	0.975	0.975	0.975	0.975
0.2	0.978	0.975	0.975	0.976	0.976
0.3	0.978	0.975	0.976	0.977	0.976
0.4	0.978	0.976	0.978	0.978	0.978
0.5	0.979	0.977	0.982	0.982	0.982
0.6	0.981	0.980	0.986	0.986	0.986
0.7	0.984	0.984	0.990	0.990	0.990
0.8	0.987	0.989	0.993	0.994	0.994
0.9	0.992	0.996	0.997	0.998	0.998
1	1.000	1.000	1.000	1.000	1.000

Note.  $nDCG$  = normalized discounted cumulative gain.

and can be widely applied. Our empirical example suggests that shifting some weight to user utility will increase user utility substantially while decreasing ad revenue only slightly. Thus, we attempt to make programmatic advertising more user-centric by explicitly trading off ad revenue to improve user utility while recommending sponsored items.

### Recommendations for Future Research

Although our model and algorithm make important contributions to the fields of advertising and RS, we believe this work is only the beginning of a much larger area for future research. We therefore provide an extended discussion of open research questions. First, our model should be tested on data sets from different industries and with field tests. We need to develop a better understanding of how often platforms can increase user utility substantially while reducing ad revenue by a small amount and where to set the value of  $\gamma$  to manage the trade-off.

Second, we need to understand the relationship between user utility and consumer lifetime value (CLV). When a platform recommends items with lower utility than others, how does this affect CLV? If this relationship is understood, then the trade-off can be between ad revenue and CLV, which are both measured in the same units (e.g., dollars). This would mean that  $\gamma$  could potentially become a variable that is selected by the optimization algorithm instead of being set by the manager. Game theory (Sayedi, Jerath, and Srinivasan 2014) could also provide relevant insights as it is often used to model the stability of a system.

Third, we need a better understanding of how to handle situations where a user has high user utility for a sponsored item. For example, if the item with the highest

utility for user  $u$  is sponsored, should the system show a “sponsored” label? On one hand, showing such a label can decrease the probability of purchase (Beel, Langer, and Genzmehr 2013), and the user might select a non-sponsored item providing less utility than the sponsored one. On the other hand, if the system receives ad revenue for showing an item, then the item is sponsored—and the system should be transparent or risk losing the trust of its users.

Fourth, note that  $a_{ui}$  is really a function of other factors. Advertising auctions tend to be second price, meaning that the highest bidder  $A$  pays the second-highest bid. This is from a game-theoretic result that keeps the auction stable, but it makes modeling revenue more complex. The second-price issue could be addressed by multiplying the highest bid by a constant that adjusts to the second-highest bid. In the proposed model, the rank is determined by user utility as well as by bid order. The ranking function is  $\text{Bid} \times P(\text{click}|Ad) = \text{expected revenue}$ . For example,  $A$  is a spammer  $P(\text{click}|A) = 0.001$ ;  $B$  is a real company  $P(\text{click}|B) = 0.1$ .  $A$  would have to bid  $100 \times B$ 's bid to win the auction, not just  $B$ 's bid plus some  $\epsilon$ , and would have to pay an amount that provides expected revenue =  $B$  for each click. The second-price criterion becomes very difficult to model under these circumstances.

Fifth, one could develop algorithms for when items have different “margins.” For example, a grocery retailer might make more profit from selling a private-label product and thus recommend it as a nonsponsored item over other items. In this case we need a separate set of constants for margin. Let  $\mu(i, r)$  be the expected margin on item  $i$  for someone with utility  $r$  (which accounts for different click probabilities). Then the objective becomes:



TABLE 5  
Example Showing Difficulty of Online Problem

User	Item	$c_{ui}$
1	<i>A</i>	3
1	<i>B</i>	2
2	<i>A</i>	5
2	<i>B</i>	2

$$Q_2 = \left[ \gamma \sum_{u \in \mathcal{U}} \sum_{i \in \mathcal{I}} \hat{r}_{ui} x_{ui} + (1-\gamma) \sum_{u \in \mathcal{U}} \sum_{i \in \mathcal{I}} (\mu(i, \hat{r}_{ui}) + a_{ui}) x_{ui} \right]$$

Sixth, one could also optimize over  $s_{\max}$ . Small  $s_{\max}$  restricts ad inventory, which will likely increase auction bids and thus the ad revenue per slot, whereas larger values of  $s_{\max}$  increase the supply of ad inventory and reduce bid amounts. This raises the possibility of reducing sponsored ad inventory without reducing revenue. One would need to know the elasticities of the supply and demand curves, which could be an important study on its own.

Seventh, we need to study the online situation, where users arrive over time and the platform does not know which ones will visit. A simple example will illustrate the problem. Suppose that we are to recommend  $k = 1$  item and that there are  $n = 2$  items, each of which is sponsored and with enough budget for exactly one exposure today (see Table 5 for criterion values). Suppose that user 1 visits the platform first, and so showing item *A* is optimal because  $c_{1A} = 3 > 2 = c_{1B}$ . Next, user 2 visits, but because *A* has exhausted its ad budget, item *B* is shown, giving  $c_{2B} = 2$  and a total criteria of  $3 + 2 = 5$ . The optimal solution to the offline problem, however, is to show user 1 item *B* and user 2 item *A*, giving a total criteria of  $5 + 2 = 7 > 5$ . Search advertising faces the same issue (Leskovec, Rajaraman, and Ullman 2014), and methods such as the Balance algorithm have been proposed (Kalyanasundaram and Pruhs 1996). Perhaps Balance could be used in the sponsored recommendation situation after substituting  $c_{ui}$  for click-through rates, but the details should be carefully thought out.

Eighth, work could be done to improve the efficiency of the algorithm. The example from Table 5 also illustrates why the sorting in the algorithm must be done over all  $mn$  items to find an optimal solution. Sorting within a user, as in the example, or within items may lead to a suboptimal solution. While sorting has superlinear computational complexity and is therefore possible for large data sets, there might be ways improve the efficiency. For example, the slowest part of the algorithm is the sort, which can be sped up by reducing the number ( $mn$ ) of user-item  $c_{ui}$  values. If the inventory is, say, 10% of  $mn$ , one could drop all values less than, say, the 85th

percentile, reducing the sort cost substantially. Knowing percentiles, however, requires sorting, unless the shape of the distribution is known. The  $c_{ui}$  values for the grocery data tend to be moderately right-skewed, say, chi-squared with 3 *df*. The mean, variance, and other moments could be found with a single pass through the list, for example, while computing  $c_{ui}$ . Using quantiles from the chi-squared distribution would give the quantiles without sorting, which could then be used to drop user-item pairs with small  $c_{ui}$  prior to sorting.

## Implications for Advertising

Over the past decade many platforms (e.g., Google, Facebook) have grown quickly to become very large companies, dominant in their industries. Advertising budgets are shifting from traditional media to platforms, which are growing quickly. We point out two features of platforms that have broader implications for the future of advertising. First, platforms are data-rich environments that enable precise targeting and personalization. Consequently, ads will become more like RS because they are moving into these platforms. Second, platforms are successful because they become the first destination for users by providing value: There is an overabundance of choice of digital “items” (information, goods, services, etc.), and the platform helps users find the items that are most relevant, across providers. They receive financial payments from providers for referrals, which could be sponsored. While these revenue streams are attractive, platforms should remember that the heart of their value proposition is being the first destination for users (Malthouse et al. forthcoming), which requires offering something of value to them. Our MRS can help manage this trade-off.

The fields of advertising and RS have developed independently of each other, and the two have starkly different underlying philosophies: The goal of advertising has been to persuade, while the goal of RS has been to help users find items of interest to them (see also Jones 1990). The ultimate goal—selling a product or, more generally, increasing CLV—may be the same, but the approaches are completely different. A more general question is whether this hybrid approach could be applied to other areas of advertising: Can media selection and targeting work better by explicitly considering user utility? We believe this is a profoundly important question, as users find new ways to avoid ads.

## NOTES

1. We do not allow  $\gamma = 0$  because then the algorithm would have no way of allocating nonsponsored items when, for example,  $s_{\max} < k$ . When  $\gamma$  is very small, e.g.,  $\gamma = 10^{-8}$ , then up to  $s_{\max}$  sponsored items are selected based on the ad revenue, and the remaining nonsponsored items, which have ad revenue equal to

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0 causing the ad revenue term in (2) to equal 0, are selected based on user utility. Constraining  $\gamma > 0$  also addresses other degenerate cases, such as not having enough sponsored items to fill  $m_{s_{\max}}$  slots.

2. Sometimes it is more convenient to express this constraint as an upper bound on the fraction of sponsored items rather than the number. In such cases, one can compute  $s_{\max}$  by multiplying the upper-bound fraction by  $k$  and using the algorithm as stated.
3. Cosine similarity is one of the most commonly used measures of the similarity between two users. If we think of each user's ratings as  $n$ -vector, it is the cosine of the angle between them. When user ratings are centered to have mean 0 for each user, cosine similarity is the Pearson correlation between the row vectors. Values near 1 indicate highly similar users, while values near 0 mean low similarity.

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